Swing-Free Transporting of Two-Dimensional Overhead Crane Using Sliding Mode Fuzzy Control

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Abstract—An adaptive sliding mode fuzzy control approach is proposed for a two-dimensional overhead crane. System linearization transforms the two-dimensional system to two independent systems: X-direction transport system and Y-direction transport system. Both the two systems are with the same dynamic model and both include two subsystems: positioning subsystem and anti-swing subsystem. A sliding mode fuzzy control approach is proposed for both X-direction transport and Y-direction transport, and it combines SMC's robustness and FLC's independence of system model. According to the influences on system dynamic performance, both of the slope of sliding mode surface and the relationship between subsystems are automatically tuned by real time fuzzy inference respectively. The effectiveness of the proposed with control is demonstrated by experiments two-dimensional prototype overhead crane.

I. INTRODUCTION

Overhead crane works as a robot in many places such as workshops and harbors to transport all kinds of massive goods. It is desired for the overhead crane to transport its payloads to the required position as fast and as accurately as possible without collision with other equipments. Moreover, the payload swing angle should be kept as small as possible.

Many works have been done in controlling the overhead crane. Park [1] and Singhose [2] adopted input shaping control method. But the input shaping must be pre-calculated accurately according to the system model. These approaches lacked robustness to external disturbances and couldn't damp residual swing well. Moreover, zero initial condition must be satisfied. Lee [3] and Giua [4] proposed feedback control methods. Besides needing accurate system model and onerous matrix computation, the above methods were greatly affected by system linearization and system parameters uncertainty.

Fuzzy logic control (FLC) is independent of system model and has some robustness. Lee [5] used fuzzy logic only in anti-swing control and applied position servo control for positioning and swing damping. Hua [6] only studied anti-swing control with fuzzy logic and didn't take positioning control into consideration. Nalley [7] adopted fuzzy logic to both positioning control and swing damping. However, because of the large number of fuzzy rules, it was difficult to set both rules and parameters of the controller only according to experiences.

Sliding mode control (SMC) is a robust design methodology using a systematic scheme based on a sliding mode surface and Lyapunov stability theorem. The main advantage of SMC is that the system uncertainties and external disturbances can be handled under the invariance characteristics of system's sliding mode state with guaranteed system stability. Er [8], Kakoub [9] and Hasanul [10] used the variable structure control (VSC) with sliding modes to control the overhead crane. In [8] and [9], the VSC was used to the positioning control and hoisting control, but another state feedback control scheme must be added for payload swing damping control. In [10], a reference model was defined to track, and the system model must be linearized. All the above VSC methods have difficulties in automatically tuning the relationship between positioning control and anti-swing control.

This paper presents a practical solution to analyze and control the overhead crane. The payload swing and crane motion of two transport directions are considered. Now that SMC is capable of tackling non-linear system with parameter uncertainties and external disturbances, and fuzzy logic control is independent of system model, crane system model is built to analyze system control characteristics without taking external disturbances (such as winds) and system parameters varying (such as different goods) into consideration. A sliding mode fuzzy control algorithm is designed for both X-direction and Y-direction transports of the overhead crane. Combining SMC's robustness and FLC's independence of system model, the proposed control law can guarantee a swing-free transportation.

The remainder of this paper is organized as follows. In

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section 2, the dynamic model of 2-dimensional overhead crane is built, the linearized model is derived and a conclusion is obtained that two-dimensional overhead crane can be divided into two independent transport systems. In section 3, an adaptive fuzzy sliding mode control algorithm is proposed for both X-direction and Y-direction transportations. In section 4, the proposed algorithm is validated through experiments. Finally, in section 5, conclusions are drawn.

II. DYNAMIC MODEL OF OVERHEAD CRANE

In this section, the system description of two-dimensional overhead crane will be given and its dynamic model will be built. Then the model will be transformed by linearization and state feedback to a system that is composed of two transport systems with the same structure. In this way, the system control and its implementation are simplified.

A. System Description

Figure 1 shows the coordinate system [11] of a two-dimensional overhead crane and its payload. XYZ is the inertial coordinate system, M_X and M_Y respectively are the X-direction trolley mass and Y-direction trolley mass including the moment-of-inertia of the gear train and motors. θ is the swing angle of the payload in XYZ space and it has two components θ_X and θ_Y . θ_X and θ_Y are the swing angle projected on XZ plane and YZ plane respectively. Assume the dynamic model has the characteristic that the payload and the trolley are connected by a massless, rigid link.

B. System Dynamics

According to Lagrangian equation:

$$\frac{d}{dt}\left(\frac{\partial L}{\partial \dot{q}_i}\right) - \frac{\partial L}{\partial q_i} = T_i \quad (i = 1, 2, 3, 4) \tag{1}$$

where, L = K - U, *K* is system kinetic energy, *U* is system potential energy, q_i is generalized coordinate (here is *x*, *y*, θ_x or θ_y), and T_i is external force (here is f_x or f_y) ($T_3=T_4=0$). The motion equations of the overhead crane system can be obtained with respect to the generalized coordinates *x*, *y*, θ_x and θ_y .

$$(M_{X} + m)\ddot{x} + ml\ddot{\theta}_{X}\cos\theta_{X}\cos\theta_{Y} - ml\ddot{\theta}_{Y}\sin\theta_{X}\sin\theta_{Y} -ml\dot{\theta}_{X}^{2}\sin\theta_{X}\cos\theta_{Y} - ml\dot{\theta}_{Y}^{2}\sin\theta_{X}\cos\theta_{Y}$$
(2)
$$-2ml\dot{\theta}_{X}\dot{\theta}_{Y}\cos\theta_{X}\sin\theta_{Y} = f_{X} - D_{X}\dot{x}$$

$$(M_{Y} + m)\ddot{y} + ml\ddot{\theta}_{Y}\cos\theta_{Y} - ml\dot{\theta}_{Y}^{2}\sin\theta_{Y} = f_{Y} - D_{Y}\dot{y} \quad (3)$$

$$ml^{2}\dot{\theta}_{X}\cos^{2}\theta_{Y} + ml\ddot{x}\cos\theta_{X}\cos\theta_{Y} + mgl\sin\theta_{X}\cos\theta_{Y}$$

$$-2ml^{2}\dot{\theta}_{X}\dot{\theta}_{Y}\sin\theta_{Y}\cos\theta_{Y} = 0$$
(4)

$$ml^{2}\ddot{\theta}_{Y} + \ddot{y}ml\cos\theta_{Y} + mgl\sin\theta_{Y}\cos\theta_{X} -ml\ddot{x}\sin\theta_{X}\sin\theta_{Y} + ml^{2}\dot{\theta}_{X}^{2}\cos\theta_{Y}\sin\theta_{Y} = 0$$
(5)



Figure 1 Two-Dimension Overhead Crane

where D_X and D_Y respectively denote the viscous damping coefficients of the crane in the X and Y directions, f_X and f_Y are the external forces on the overhead crane in the X and Y directions, respectively.

C. System Model Analysi

In industry, the maximum acceleration of the overhead crane is set smaller than the gravitational acceleration. For safety considerations, the rope length is usually kept constant when the overhead crane is in motion. For small swing around the vertical equilibrium, $\sin \theta_X \approx \theta_X$, $\sin \theta_Y \approx \theta_Y$, $\cos \theta_X \approx 1$ and $\cos \theta_Y \approx 1$. In addition, $\sin \theta_X \sin \theta_Y \approx 0$, $\dot{\theta}_X^2 \approx 0$, $\dot{\theta}_Y^2 \approx 0$ and $\dot{\theta}_X \dot{\theta}_Y \approx 0$ also hold for small swing. The nonlinear model can be simplified to the following linearized model:

$$(M_{X} + m)\ddot{x} + ml\theta_{X} = f_{X} - D_{X}\dot{x}$$

$$l\ddot{\theta}_{X} + \ddot{x} + g\theta_{X} = 0$$
(6)

$$(M_{Y} + m)\ddot{y} + ml\ddot{\theta}_{Y} = f_{Y} - D_{y}\dot{y}$$

$$l\ddot{\theta}_{Y} + \ddot{y} + g\theta_{Y} = 0$$
(7)

In practice, the crane is normally driven by servo-motors. The servomotor has three control modes: position control, speed control and torque control. In order to simplify the system dynamic model, the speed control mode is used. Through the following state feedback transformations:

$$u_X = (M_X + m)^{-1} (f_X - D_X \dot{x} - ml\theta_X)$$

$$u_Y = (M_Y + m)^{-1} (f_Y - D_Y \dot{y} - ml\theta_Y)$$
(8)

the system model can be described as

$$\ddot{x} = u_X l\ddot{\theta}_X + u_X + g\theta_X = 0$$
⁽⁹⁾

$$\ddot{y} = u_{y}$$

$$l\ddot{\theta}_{y} + u_{y} + g\theta_{y} = 0$$
(10)

The linearized dynamic model consists of the X-direction transport dynamics and Y-direction transport dynamics. The X-direction dynamics and Y-direction dynamics are decouped and with the same structure. Therefore, the same control algorithm can be designed for both the X and Y direction transport systems. For this system model, the system control input is the acceleration of the overhead crane.

Because the viscous damping and the masses of trolleys and payload maybe are not known and the above transform makes the model be independent of them, the system control is easily implemented in practice.

III. CONTROL DESIGN

In this section, an adaptive slide mode fuzzy controller will be designed for the two-dimensional overhead crane. Assume the desired state is generalized coordinates origin. Since the two-dimensional overhead crane can be decouped into two independent transport systems, a control algorithm will be designed for both of them. Only the X-direction transport system is considered below.

A. Sliding mode fuzzy control (SMFC)

Consider a second-order system of the form as follows:

$$\begin{aligned} x_1 &= x_2 \\ \dot{x}_2 &= f(X) + b(X)u \end{aligned}$$
(11)

where, $X=(x_1, x_2)$ is state variable vector, f(X) and b(X) are continuous linear or nonlinear functions, u is the control input. A sliding mode function can be defined as

$$s = x_2 + \lambda_1 x_1 \tag{12}$$

Very similar to sliding mode control with boundary layer, the control input on the two sides of the sliding mode surface are opposite in sign and its magnitude is proportional to the distance between the state vector and the sliding mode surface. Therefore, the sliding mode fuzzy control is designed to:

R_i : IF s IS F_i THEN u IS U_i

where F_i is the linguistic value of *s* in the *i*th-fuzzy rule, and U_i is the linguistic value of *u* in the *i*th-fuzzy rule. The fuzzification of the sliding mode function is illustrated in Fig.2

B. Adaptive sliding mode fuzzy control (ASMFC)

The X-direction transport systems can be represented as: $\dot{x}_1 = x_2$

$$\dot{x}_{2} = f_{1}(X) + b_{1}(X)u$$

$$\dot{x}_{3} = x_{4}$$

$$\dot{x}_{4} = f_{2}(X) + b_{2}(X)u$$
(13)

where, $X=(x_1, x_2, x_3, x_4)$ is the state variable vector that include crane position, velocity, payload swing angle and angular velocity, $f_1(X)$, $f_1(X)$, $b_1(X)$ and $b_2(X)$ are continuous nonlinear functions, u is the control input.



Figure 2 Fuzzification of sliding mode function in sliding mode fuzzy control

From (13), the X-direction transport system has two coupled subsystems: positioning subsystem and anti-swing subsystem. In order to decouple the system, two sliding mode functions are defined for the two subsystems:

$$s_1 = x_2 + \lambda_1 x_1 \tag{14}$$

$$s_2 = x_4 + \lambda_2 x_3 \tag{15}$$

where λ_1 and λ_2 are positive real numbers.

System performance is very sensitive to the slope λ_1 (or λ_2) of the sliding mode function: when the value of λ_1 (or λ_2) becomes larger, the rise-time will become smaller, but at the same time, both overshoot and tuning-time will become larger, and vice versa. So a law is designed to adjust the slope λ_1 (or λ_2) of the sliding mode function in real time: when system state errors are large, a bigger slope of the sliding mode function is used in order to make the system state approach the sliding mode surface and equilibrium point. This is because the convergence speed on the sliding mode surface is high if a large λ_1 (or λ_2) is used. In mechanical systems, the value of λ_1 (or λ_2) is typically limited by three factors: the frequency of the lowest unmodelled structural mode, the largest unmodelled time delay, and the sampling rate.

According to the mechanical system limitation, the slope of the sliding mode function is given for the *l*th subsystem (l=1 or 2) by

$$\lambda_l = \lambda_l^b + B_l \Delta \lambda_l \tag{16}$$

where, λ_l^b is the basic value of λ_l , B_l is the tuning scope of λ_l , and $\Delta \lambda_l$ is the tuning variable. The value of $\Delta \lambda_l$ can be obtained according to the following fuzzy rules:

$$R_i$$
: IF $|x_{2l-1}|$ IS $A_l^{\ i}$ THEN $\Delta \lambda_l$ IS $\Delta \lambda_l^{\ i}$

where, R_i is the *i*th item of *m* rules, A_l^i is a fuzzy set of input variable $|x_{2l-1}|$, and $\Delta \lambda_l^i$ is a fuzzy set of output variable $\Delta \lambda_l$. The output singleton fuzzy sets and the center-of-gravity

defuzzification method are used:

$$\Delta \lambda_{l} = \left(\sum_{i=1}^{m} \mu_{A_{l}^{i}}(|x_{2l-1}|) \times \Delta \lambda_{l}^{i}\right) / \sum_{i=1}^{m} \mu_{A_{l}^{i}}(|x_{2l-1}|)$$
(17)

 $\mu_{A_i^t}(|x_{2^{l-1}}|)$ is the firing degree of the *i*th rule.

The composite sliding mode function can be defined as

$$s = s_1 + \lambda s_2 = x_2 + \lambda_1 x_1 + \lambda (x_4 + \lambda_2 x_3)$$
(18)

where λ is a negative real number. Tuning the coefficient λ can adjust the function of the positioning subsystem and the anti-swing subsystem on the sliding mode function. When λ becomes smaller, the positioning subsystem is strengthened; and when λ becomes larger, the anti-swing subsystem is strengthened. So another fuzzy inference is designed: if system state is far from sliding mode surface $s_2=0$, a larger value of λ is adopted, vice versa. As the tuning of the sliding mode function slope, let

$$\lambda = \lambda^b + B\Delta\lambda \tag{19}$$

where, λ^{b} is the basic value of λ , *B* is the tuning scope of λ , and $\Delta\lambda$ is the tuning variable. The value of $\Delta\lambda$ can be obtained according to the following fuzzy rules:

R_j : IF $|s_2|$ IS F_2^j THEN $\Delta\lambda$ IS $\Delta\lambda_j$

where, R_j is the *j*th item of *n* rules, F_2^{j} is a fuzzy set of input variable $|s_2|$, and $\Delta \lambda_j$ is a fuzzy set of output variable $\Delta \lambda$. The output singleton fuzzy sets and the center-of-gravity defuzzification method are used:

$$\Delta \lambda = \left(\sum_{j=1}^{n} \mu_{F_{2}^{j}}\left(|s_{2}|\right) \times \Delta \lambda^{j}\right) / \sum_{j=1}^{n} \mu_{F_{2}^{j}}\left(|s_{2}|\right)$$
(20)

where $\mu_{E^{j}}(|s_{2}|)$ is the firing degree of the *j*th rule.

Only in the anti-swing subsystem of the X-direction transport system, the slope of the sliding mode function is automatically adjusted by fuzzy inference system, which is called as adjustor 1. The relationship between the positioning subsystem and anti-swing subsystem are automatically tuned by another fuzzy inference system, which is called as adjustor 2. For the X-direction transport system of the overhead crane, the composite sliding mode function s works as the input to the sliding mode fuzzy control. The fuzzy rules are:

$$R_k$$
: IF s IS F_k THEN u_f IS U^k

where, R_k is the *k*th item of *p* rules, F^k is a fuzzy set of input variable *s*, and U^k is a fuzzy set of output variable u_f . The output singleton fuzzy sets and the center-of-gravity defuzzification are used:

$$u_{f} = \left(\sum_{k=1}^{p} \mu_{F^{k}}(s) \times U^{k}\right) / \sum_{k=1}^{p} \mu_{F^{k}}(s)$$
(21)

where $\mu_{F^k}(s)$ is the firing degree of the *j*th rule and u_f is the

output of the adaptive sliding mode fuzzy controller.

Now consider the reaching condition of the sliding mode surface that is based on the flowing Lyapunov function:

$$V = s^2/2 \tag{22}$$

By taking the time derivative of equation (18) and substituting into equation (22), it is easy to obtain from equation (13)

$$s\dot{s} = s(f_1(X) + \lambda f_2(X) + \lambda_1 x_2 + \lambda \lambda_2 x_4) + (b_1(X) + \lambda \lambda_2 b_2(X))su$$
(23)

Form equation (9), we can see: $b_1(X)$ and λ_2 is positive, and $b_2(X)$ is negative. When λ is negative, the term in equation (23), $b_1(X) + \lambda b_2(X)$ are always positive. Therefore, increasing the control input *u* will result in decreasing *ss* as the sliding mode function *s* is negative, and decreasing the control input *u* will result in decreasing *ss* as the sliding mode function *s* is positive.

Remark 1: According to the system dynamic model that the X-direction transport system and Y-direction transport system are decoupled and with the same linearized model, the control algorithm is also applicable to Y-direction transport system.

Remark 2: The proposed control design is independence of the linearized system model, i.e. the control algorithm is designed for nonlinear overhead crane system. The linearized model derived in section 2 is used to explain the two-dimensional overhead crane consisting of two approximately independent transport systems.

Remark 3: When the initial payload angles are zeros, both X-direction and Y-direction transportations will arrive at the goal at the same time with the same adaptive sliding mode fuzzy controller.

Remark 4: Now that the servomotors adopt speed control mode while the output of the controller is acceleration, actual input of the servomotors is:

$$u = \int_{t_0}^{t_c} u_f dt \tag{24}$$

where t_0 and t_c are initial time and current time separately.

The control scheme is illustrated in figure 3.

IV. EXPERIMENT RESULTS

To confirm the effectiveness of the proposed control algorithm, some experiments have been performed with a two-dimensional prototype overhead crane illustrated in Figure 4. The prototype consists of two sets of components that include mechanical system, data sampling system, and control system. For the mechanical system, the trolleys are driven by AC servomotors, and the payload is connected to a cable that is attached to the underside of the trolley, where two precise angle sensors are installed to measure the swing angles of X-direction and Y-direction. The control algorithm is implemented on a Pentium III 800 MHz PC running under the Windows operating system.

In the control algorithm, the adaptive tuning of the slope of the sliding mode function is only used for the anti-swing subsystems. The parameters of the controller are as follows: $\lambda_1=0.5$, $\lambda_2^b = 2.28$, $B_2=3$, $\lambda^b = -1$, B=-4.6. The tunings of λ and λ_2 adopt the same fuzzy rules table, given in table 1. The sliding mode fuzzy rules are provided in table 2.

	Table 1 Rules table for tuning			λ and λ_2			
	_	$ e_3 $ or $ s_2 $	S	М	L		
	_	$\lambda_2 \text{ or } \Delta \lambda$	0	0.5	1		
Tab	le 2	Rules table	e of slidi	ng mode	fuzzy	cont	roller
	S	NB	NS	ZO	PS	PB	-
	u_f	2.5	1.25	0	-1.25	-2.5	-

Figure 5 and 6 show the experimental results of transport from position (-1.2, -0.6) to position (0, 0) with zero initial angles. Figure 7 shows the X-direction transport when the initial angle is not zero. In the above figures, velocity is 0.2m/s each grid in Y-axis. Figure 8, 9 and 10 show the damping swing experiment results and the control is added from the 6th second. Figure 8 is angle phase plane and figure 9 and 10 are angles time responses. From the experiment results, it is clear that the control law can make the X-direction and Y-direction transports arrive at goal at the same time when initial angle is zero, and the control law can damp swing angle at goal whether the initial angle is zero. Moreover, the control law can damp swing angle in short time while keeping position.

V. CONCLUSION

In this paper, a two-dimensional overhead crane is transformed to two independent systems that are with the same dynamic model in order to simplify the controller design. An adaptive sliding mode fuzzy control approach has been designed for both X-direction transportation and Y-direction transportation, and its effectiveness has been demonstrated by experiments on a two-dimensional prototype overhead crane. The experiments have shown the proposed control law guarantees both accurate positioning control and prompt damping of payload swing. The stability and performance of the proposed control law are guaranteed in spite of large initial swing angle.

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Figure 3 Control Scheme



Figure 4 Two-dimension Prototype Overhead Crane

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