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## Abstract

This project involves the model-based optimisation and design of tubular reactors for the production of low-density polyethylene (LDPE). Information obtained from literature and industry results in detailed but complex mathematical models, which are not directly suited for optimisation purposes. Hence a two-step strategy is proposed. In a first step, a basic model which captures the most important phenomena is constructed based on advanced model reduction techniques. This basic model is used to identify the most promising optimisation possibilities. In a second step, the optimisation is performed for different industrially relevant objectives. Depending on the objective, the reduced model will be further adjusted to the required level of detail.

## LDPE

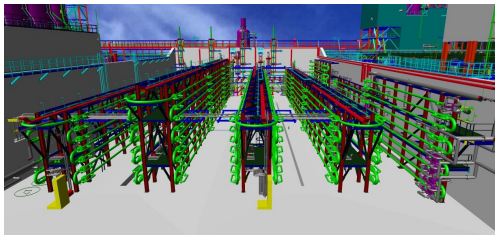
### Broad application area



## Modeling

On a different level of detail

- Macro scale: Reactor



- Micro scale: Reactions

A **complex system** of (un)correlated differential (time and space) and algebraic equations.

Using model reduction techniques like **sensitivity analysis**

A **basic model** which still contains sufficient essential information and characteristics

$$\begin{aligned} \frac{dx}{d\xi} &= f[x(\xi), u(\xi), \xi] \\ 0 &= g[x(\xi), y(\xi), u(\xi), \xi] \end{aligned}$$

## Optimisation

Optimal control problem:

$$J = h[x(\xi_f)] + \int_0^{\xi_f} g[x(\xi), u(\xi)] dt$$

Subject to:

$$\begin{aligned} \frac{dx}{d\xi} &= f[x(\xi), u(\xi), \xi] \\ 0 &= g[x(\xi), y(\xi), u(\xi), \xi] \end{aligned}$$

Heat transfer

Kinetics

Level of design detail

Re-increase in model complexity:

**Detailed objective-specific model**

$$\begin{aligned} \frac{dx}{dt} &= f_{\text{specific}}[x(\xi), u(\xi), \xi] \\ 0 &= g_{\text{specific}}[x(\xi), y(\xi), u(\xi), \xi] \end{aligned}$$